

(Terzaghi, Meyerhof, Hanen, Vesic)



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1.

(, , 가)

(failure equation)

(Murff, 1994; Bransby

and Randolph, 1998; Taiebat and Carter, Prandlt(1921)Reissner(1924) 2000).

Prandlt-Reissner

(Terzaghi,

Meyerhof, Hanen, Vesic)

가

(1) (Terzaghi, 1943; Meyerhof, 1951); (2) (Shield, 1954; Chen, 1975; Sarma, 1979; Sarma and Iossifelis, 1990; Drescher and Detournay, 1993; Michalowski, 1995; Soubra, 1999); (3) Slip-line (Sokolovskii, 1960; Hansen, 1961); (4)

2.

2.1

(Griffiths, 1982; Frydman and Burd, 1997).

Terzaghi(1943)

(1) 2.2

$$q_u = cN_c + qN_q + \frac{1}{2} BN \quad (1)$$

, c , q 가 (= 0, c =)
, B
N_c, N_q, N_r Bolton(1979)
(strip foundation)

Terzaghi

, s = 1.2

Meyerhof(1951, 1963)

Bolton (3)

Terzaghi가
, Terzaghi가

$$\frac{V}{A} = 1.2s_u \left[1 + \arcsin\left(\frac{H}{As_u}\right) + \sqrt{1 - \left(\frac{H}{As_u}\right)^2} \right] \quad (3)$$

Osborne (1991)
, Murff(1994)

Meyerhof

3

가

(4)

$$\sqrt{\left(\frac{M}{D}\right)^2 + H^2} + \frac{V^2}{V_c} - V \left(1 - \frac{V_t}{V_c} \right) + V_t = 0 \quad (4)$$

, 1, 2 , V_c, V_t

Hansen(1970) Vesic(1973)Meyerhof

V_t

(suction)

$$q_u = cN_{cs} + qN_{qs} + \frac{1}{2} BN_{sdi} + \dots \quad (2)$$

(4) (5) V_t = -V_c = -V_u 가
3V_uD 4V_u
(5) (6)

$$\sqrt{\left(\frac{M}{3V_u D}\right)^2 + \left(\frac{H}{4V_u}\right)^2 + \left(\frac{V}{V_u}\right)^2} - 1 = 0 \quad (5)$$

$$\sqrt{\left(\frac{M}{M_u}\right)^2 + \left(\frac{H}{H_u}\right)^2 + \left(\frac{V}{V_u}\right)^2} - 1 = 0 \quad (6)$$

Taiebat Carter(2000)3

[1]

, Taiebat Carter

(7)

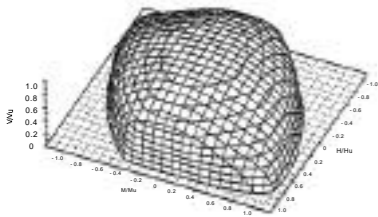
$$\left(\frac{V}{V_u}\right)^2 + \left[\frac{M}{M_u}\left(1 - \frac{HM}{H_u |M|}\right)\right]^2 + \left|\left(\frac{H}{H_u}\right)^3\right| = 1 \quad (7)$$

1 , Taiebat

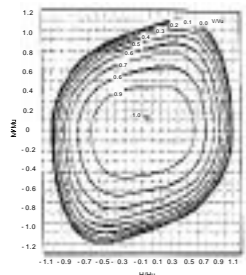
Carter 1 = 0.3

. [2] (7) 1 = 0.3

[1]



[2]



3.

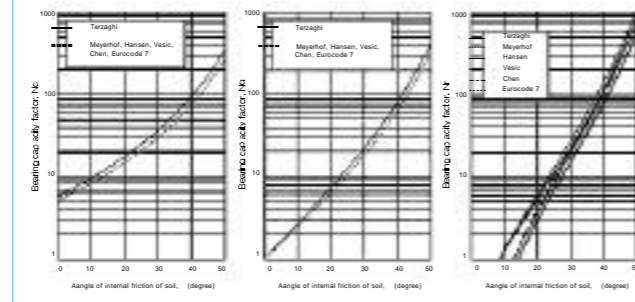
3.1

Terzaghi(1943), Meyerhof(1963), Hansen(1970), Vesic(1973), Chen(1975), Eurocode

7 < 1 > [3]

	N_q	N_c	N
Terzaghi	$\frac{a^2}{\cos^2(45 + \phi/2)}$ $a = e^{(0.75 - \phi/2)\tan\phi}$	$(N_q - 1)\cot\phi$	$\frac{\tan\phi}{2} \left(\frac{K_p}{\cos^2\phi} - 1 \right)$
Meyerhof	$e^{\tan\phi} \tan^2\left(45 + \frac{\phi}{2}\right)$	$(N_q - 1)\cot\phi$	$(N_q - 1)\tan(1.4\phi)$
Hansen	$e^{\tan\phi} \tan^2\left(45 + \frac{\phi}{2}\right)$	$(N_q - 1)\cot\phi$	$1.5(N_q - 1)\tan\phi$
Vesic	$e^{\tan\phi} \tan^2\left(45 + \frac{\phi}{2}\right)$	$(N_q - 1)\cot\phi$	$2(N_q + 1)\tan\phi$
Chen	$e^{\tan\phi} \tan^2\left(45 + \frac{\phi}{2}\right)$	$(N_q - 1)\cot\phi$	$2(N_q + 1)\tan\phi \tan\left(45 + \frac{\phi}{5}\right)$
Eurocode7	$e^{\tan\phi} \tan^2\left(45 + \frac{\phi}{2}\right)$	$(N_q - 1)\cot\phi$	$2(N_q - 1)\tan\phi$

[3] N_c, N_q, N



3.2

3.2.1

$$q_u = cN_c c_s c_i \quad (8)$$

$$N_c = \dots \quad (9)$$

, c 가

< 2 >

[4] < 2 >

가

Taiebat Carter가

가

(

) 가 [5]

Murff 가 $V/V_u - H/H_u$

$$A_v = \frac{D^2}{2} \left(\text{Arccos} \frac{2e}{D} - \frac{2e}{D} \sqrt{1 - \left(\frac{2e}{D}\right)^2} \right) \quad (9)$$

$$\frac{B_v}{L_v} = \frac{b}{l} = \sqrt{\frac{D - 2e}{D + 2e}} \quad (10)$$

, D , e

(= M / V)

(1) V-H

V-H

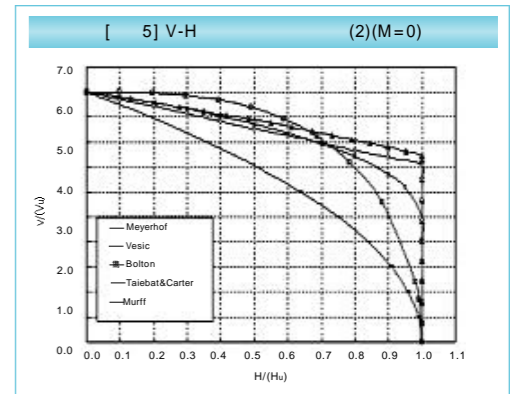
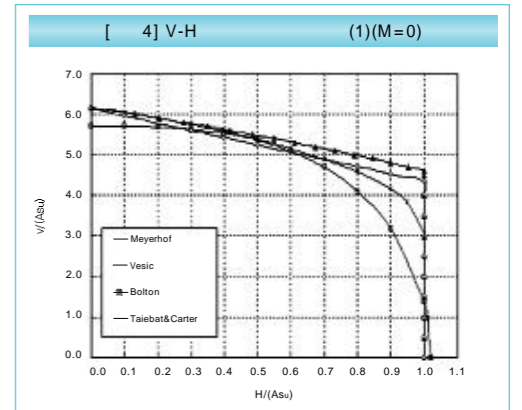
< 2 > V-H ()

Meyerhof	$\frac{H}{A_s} = \frac{V}{A_s} \tan \left[2 \left(1 - \sqrt{\frac{1}{N_c c_s} \frac{V}{A_s}} \right) \right]$ $\frac{H}{H_u} = 6.17 \frac{V}{V_u} \tan \left[2 \left(1 - \sqrt{\frac{6.17}{N_c c_s} \frac{V}{V_u}} \right) \right]$	$N_c = 5.14$ $c_s = 1.2$ $c_i = \left(1 - \frac{e}{90} \right)^2$
Vesic	$\frac{V}{A_s} = c_s \left(N_c - 1.5 \frac{H}{A_s} \right)$ $\frac{V}{V_u} = \frac{6.14}{c_s} \left(N_c - 1.5 \frac{H}{H_u} \right)$	$N_c = 5.14$ $c_s = 1.194$ $c_i = 1 - \frac{mH}{A_v c_s N_c}$
Bolton	$\frac{V}{A_s} = 1.2 \left[1 + \arcsin \left(\frac{H}{A_s} \right) + \sqrt{1 - \left(\frac{H}{A_s} \right)^2} \right]$ $\frac{V}{V_u} = 0.2 \left[1 + \arcsin \left(\frac{H}{H_u} \right) + \sqrt{1 - \left(\frac{H}{H_u} \right)^2} \right]$	
Taiebat & Carter	$\frac{V}{A_s} = 5.7 \sqrt{1 - 0.94 \left(\frac{H}{A_s} \right)^3} \left[\left(\frac{V}{V_u} \right)^2 + \left(\frac{H}{H_u} \right)^3 \right] = 1$	
Murff	$\left \frac{H}{H_u} \right + \left(\frac{V}{V_u} \right)^2 - 1 = 0$	

, V_u : (H=0, M=0)

H_u : (V=0, M=0)

S_u :



Meyerhof 가 , Taiebat Carter 가 (critical angle) < 3>

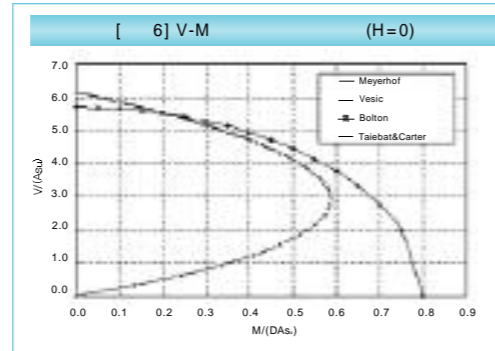
< 3>			
	(V _u)	(H _u)	
Meyerhof	6.17A _s	1.0A _s	12.2 _o
Vesic	6.14A _s	1.0A _s	13 _o
Bolton	6.17A _s	1.0A _s	18 _o
Taiebat&Carter	5.7A _s	1.02A _s	19 _o

(2) V-M

가 , (8) (9) (10) e=M/V V-M [6] Taiebat Carter 0 M_u 0.8A_s

[6] , Meyerhof, Hansen, Vesic (M_{max}) (V_u) 1/2 (e/D) 0.2 M_{max} / D = 0.095V_u (11)

(Meyerhof, Hansen, Vesic) Taiebat Carter 가



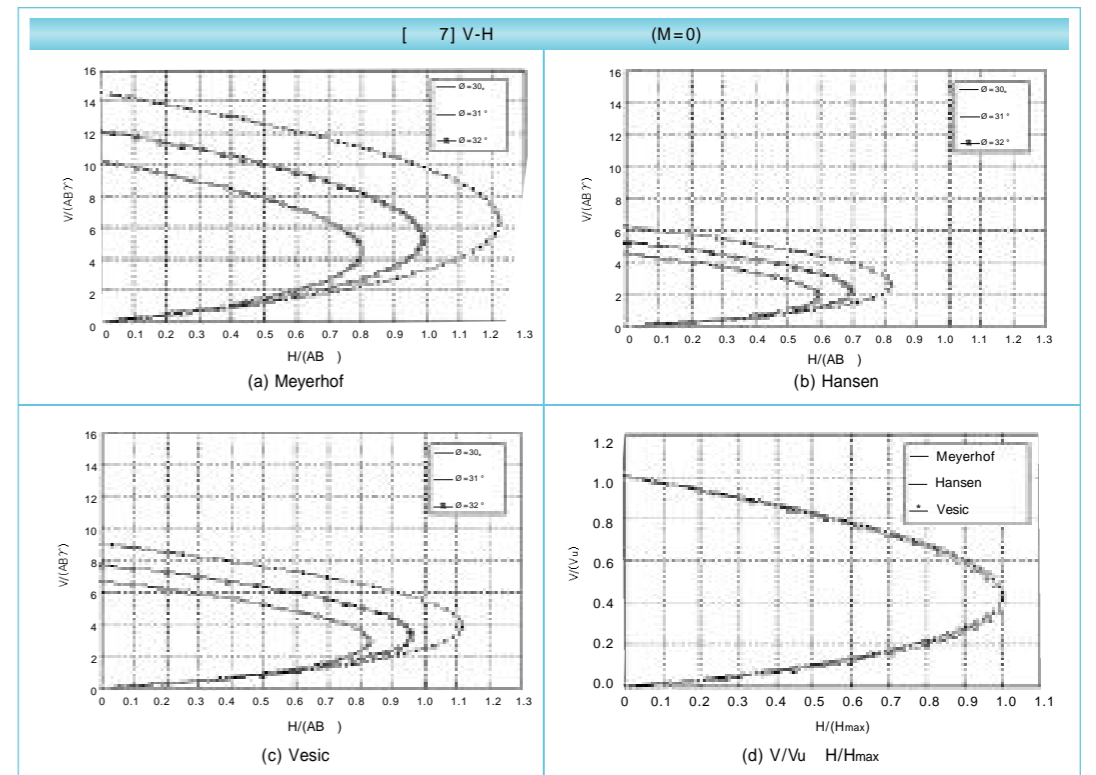
3.2.2

$$q_u = \frac{1}{2} B N_s i \quad (12)$$

N, s, i, B, 가 , < 4> [7]

< 4> V-H ()		
Meyerhof	$\frac{H}{AB} = \frac{V}{AB} \tan \left[\left(1 - \sqrt{\frac{2}{N_s} \frac{V}{AB}} \right) \right]$	$i = \left(1 - \frac{0.1}{\phi} \right)^2$
Vesic	$\frac{H}{AB} = \frac{V}{AB} \left(1 - 2.5 \sqrt{\frac{2}{N_s} \frac{V}{AB}} \right)$	$i = \left(1 - \frac{H}{V + A_s c_a \cot \phi} \right)^{m+1}$ m = 2.5, c _a = 0
Hansen	$\frac{H}{AB} = \frac{1}{0.7} \frac{V}{AB} \left(1 - 3.5 \sqrt{\frac{2}{N_s} \frac{H}{AB}} \right)$	$i = \left(1 - \frac{0.7H}{V + A_s c_a \cot \phi} \right)^2$ z = 3.5, c _a = 0

() 30°, 31°, 32° 가 , Vesic Hansen H_{max}/V_u [7] V/V_u H/H_{max} Meyerhof 45° 55° Vesic Hansen



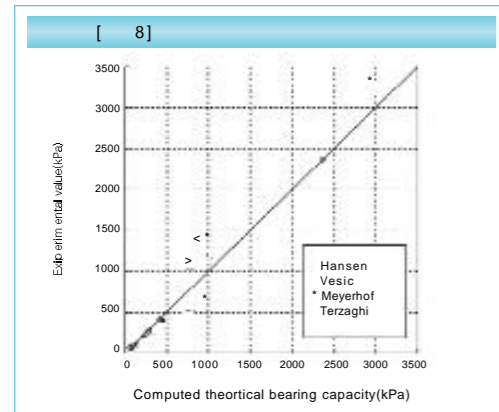
< 5> (V _u) (H _{max})					
				V _u /H _{max}	
Meyerhof	30 _o	10.19 AB	0.80 AB	0.08	30 _o
	31 _o	12.18 AB	0.99 AB		31 _o
	32 _o	14.60 AB	1.22 AB		32 _o
Vesic	30 _o	4.52 AB	0.59 AB	0.13	45 _o
	31 _o	5.31 AB	0.70 AB		
Hansen	30 _o	6.72 AB	0.83 AB	0.12	55 _o
	31 _o	7.80 AB	0.96 AB		
	32 _o	9.06 AB	1.12 AB		

Test No.	(m)	(m)	(m)	(kN/m ³)	(°)	(kPa)	(kPa)	
1	0	0.5	2	15.69	39	6.37	1059.48	Muhs
2	0.5	0.5	2	16.38	36	3.92	1196.82	
3	0.5	0.5	2	17.06	41	7.8	2374.02	
4	0.5	1	1	17.06	39	7.8	3237.30	
5	0.4	0.71	0.71	17.65	22	12.75	402.21	Milovic
6	0.5	0.71	0.71	17.65	25	14.7	539.55	
7	0	0.71	0.71	17.06	20	9.8	215.82	
8	0.3	0.71	0.71	17.06	20	9.8	255.06	
9	0	0.1015	0.127	17.16	40	0	316.00	Yetimoglu
10	0	0.05	0.2	16.6	44	0	67.60	Leshchinsky
11	0	0.0381	0.2	16.6	44	0	63.25	
12	0.01	0.05	0.2	16.6	44	0	95.60	

4. 1) N_q, N_c

Milovic, Muhs, Yetimoglu Leshchinsky

< 6> [8]



5. 2) Meyerhof, Vesic 12.2, 13.0 °

, Taiebat Carter 3

19° V-M

Taiebat Carter

3)

, Terzaghi 가

가 가

(H_{max})

, Vesic, Meyerhof, 가

Hansen (V_u) 8%,

13%, 12%

4)

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